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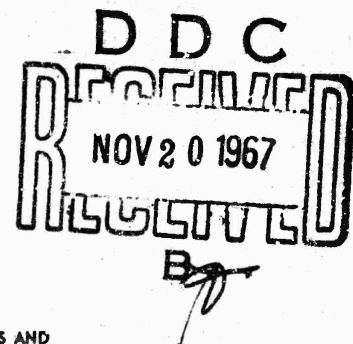
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EXPERIMENTAL AND THEORETICAL KINETICS OF HIGH TEMPERATURE FLUOROCARBON CHEMISTRY

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Prepared jointly for

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DEPUTY FOR REENTRY SYSTEMS
AIR FORCE SYSTEMS COMMAND
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by

(10) Anthony P. Modica

APPROVED

J. A. Luceri, Manager
REST Program

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ABSTRACT

Ultraviolet absorption was used to measure the rate of formation of difluoro-methylene (CF_2) from decomposed CF_3I, C_2F_6, and CF_4 in excess argon behind shock waves. In some experiments pure CF_4 was shocked. Data were taken over a temperature range from 1700° to 3000° K at total concentrations between $2(10^{-5})$ and $5(10^{-6})$ mole-cm^{-3}. A chemical, nonequilibrium shock-tube computer program was developed to analyze the CF_2 kinetic profiles. By curve fitting the data, rate constants for a number of fluorocarbon reactions are obtained.

Unclassified report

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Foreword

This report presents work performed by the Chemical Physics Research Group of
the Aerophysics Laboratory of the Avco Corporation Missile and Space Systems
Division, 201 Lowell Street, Wilmington, Massachusetts. The present task has been
supported jointly by the Space and Missile Systems Organization (SAMSO), Deputy
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The Air Force monitor for the ABRES REST Program is Capt. W. Mercer, SMYSE,
USAF, Project Officer.

This technical report has been reviewed and is approved.

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Capt. W. Mercer, SMYSE
REST Project Office
Space and Missile System Organization
Norton Air Force Base, California

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INTRODUCTION

The role of fluorine in the high temperature oxidation chemistry of tetrafluoro-ethylene (C_2F_4) is little understood. For example, among the reaction products of C_2F_4 and its polymer with oxygen, there have been identified CF_4 and CF_3 species.[1,2] It was suspected that these molecules resulted from the reaction between fluorine and the difluoromethylene radical (CF_2). Support of this hypothesis was noted when shock heated mixtures of CF_3I, C_2F_6 and CF_4 in argon diluent as well as pure CF_4 were found to decompose to CF_2. Experiments were carried out to detect the CF_2 radical by its absorption in the ultraviolet. In the present paper, measured kinetic profiles of this species are analyzed with a computer program. The computer program solves simultaneously the Hugoniot relations (mass, momentum, and energy) and the chemical rate equations for a chemically unrelaxed shock wave. The calculated rate profiles of CF_2 are compared with experiment. Some of the rate constants employed in the analysis were taken from literature sources, some were determined empirically and others were estimated from theory or deduced from JANAF equilibrium constants.

EXPERIMENTAL MEASUREMENTS

The shock-tube apparatus has been described previously.[1] It consists of 1.5-inch inside diameter stainless steel sections provided with light screens for shock velocity measurements and an optical station for ultraviolet absorption spectroscopy. Gas mixtures of CF_4 (Matheson, 95 percent purity), CF_3I (Air Products, 98 percent purity), C_2F_6 (Air Products, 99.9 percent) in excess argon (Matheson, 99.999 percent purity) were prepared for study. A few tests were conducted in undiluted CF_4. The CF_2 radicals in the shock-heated reaction mixtures were followed photometrically in absorption at 2660Å. The absorption coefficient, 1.15×10^6 (±10 percent) cubic centimeter per mole-centimeter, was used to calculate concentration from Beer's law.[3] Oscillogram records shown in Figure 1 are typical of the CF_2 absorption from these gas mixtures. The CF_3I and C_2F_6 molecules were studied since CF_3 radicals are immediately formed behind the shock wave, making the rate determining step for CF_2 appearance the dissociation of CF_3. With CF_4, the complete fluorocarbon chemistry involving CF_4, CF_3 and CF_2 is given. By studying the decomposition rates leading to CF_2, the kinetics of the fluorine oxidation reactions may thus be ascertained from detail balancing with appropriate equilibrium constants.

NONEQUILIBRIUM SHOCK TUBE PROGRAM

The equations governing a moving one-dimensional inviscid fluid in a shock tube are the so-called Rankine-Hugoniot[4] relations expressing conservation of mass, momentum, and energy,

$$d(\rho u)/dt = 0 \qquad (mass) \qquad\qquad (1)$$

$$\rho u \, d(u + \frac{p}{\rho u})/dt = 0 \qquad (momentum) \qquad\qquad (2)$$

$$\rho u \, d(h + 1/2 \, u^2)/dt = 0 \qquad (energy) \qquad\qquad (3)$$

where ρ is the density, u is the flow velocity, p is pressure and h is the enthalpy per unit mass. For a multi-component gas h is defined by

$$h = \frac{\Sigma \, c_i \, h_i}{\Sigma \, c_i \, M_i} \qquad\qquad (4)$$

The quantity c_i is the concentration of the ith species in mole per cubic centimeter, h_i is the molar enthalpy and M_i the gram molecular weight. The ideal gas equation

$$p = \frac{\rho \, \Sigma \, c_i}{\Sigma \, c_i M_i} \, RT \qquad\qquad (5)$$

is used to relate the thermodynamic temperature T to pressure and density where R is the universal gas constant per mole. The molar enthalpy is then expressed in terms of temperature by a power series,

$$h_i = \left(L_1 T + \frac{L_2 T^2}{2} + \frac{L_3 T^3}{3} + \frac{L_4 T^4}{4} - L_5 T^{-1} + L_6 \right)_i \qquad\qquad (6)$$

A curve fit of the molar enthalpy of each species was generated from JANAF thermochemical data.[5] The variation in species concentration resulting from chemical reaction and volumetric change behind the shock wave is given by

$$\frac{dc_i}{dt} - \frac{c_i}{\rho} \frac{d\rho}{dt} = \Sigma \, \pi \, \nu_{kj} \, c_{k_j} \, A_{fj} \, T^{n_j} \, exp \, (E_{fj}/RT)$$

$$- \, \Sigma \, \pi \, \nu_{ij} \, c_{i_j} \, A_{rj} \, T^{n_j} \, exp \, (E_{rj}/RT) \, , \qquad\qquad (7)$$

where the positive term on the right of the equality reflects the sum of the chemical rates leading to species production and the negative term, the rates for removal. Subscripts f and r denote the forward and reverse processes, ν_{kj} and ν_{ij} are the stoichiometric coefficients for the kth and i^{th} species in the jth reaction; A_j, n_j and E_j are the pre-exponential factor, temperature exponent, and activation energy of the rate constant for that reaction. To solve this set of differential equations for a multicomponent, chemically relaxing shock wave, a Runge-Kutta integration scheme[6] and an IBM 360 computer were employed. The inputs to the calculation are the shock velocity, state of the gas ahead of the shock wave, the chemical reactions to be considered, the forward and reverse rate constants, and coefficients of the enthalpy curve-fits. Typical machine times for solving the fluorocarbon chemical kinetics problems ran between 1 and 2 minutes. Before using the nonequilibrium shock-tube program to analyze the present data, a program check was made against an air chemistry, stream tube program developed by McNamin and O'Brien.[7] Figure 2 shows that calculations from both programs for electron density behind a shock wave into air agree numerically to within 3 percent.

CHEMICAL MECHANISMS AND KINETICS

The reactions considered in this study are shown in Table 1.

CF_3I and C_2F_6 Decomposition: A bimolecular rate constant for R1 was estimated from classical collision theory[8] assuming energy contributions from half the number of vibrational modes and a steric factor of 0.1. The dissociation rate constant of R2 was obtained from the JANAF equilibrium constant and the rate constant of Ayscough[9] for trifluoromethyl radical recombination. Calculations based on these rate constants (Figures 3 and 4) showed that within a few microseconds after shock passage CF_3I was dissociated by several orders of magnitude and that C_2F_4 was about 80 percent dissociated with R2 and R2' in equilibrium. Under these conditions, the apparent rate constant for CF_2 formation by CF_3 dissociation (R3) is given by

$$\frac{d[CF_2]}{\rho_{21} \, dt_\ell} = k_3 \, (expt'l) \, \{[CF_3]_0 - (1+\gamma) \, [CF_2]\} \, [Ar] \tag{8}$$

where γ is zero if $R4' \ll R3$ and one if $R4' \gg R3$, i.e., for each CF_2 produced one CF_3 radical is removed when fluorine attachment is slow and two CF_3 radicals are removed when fluorine attachment is fast. The concentration of CF_3 initially behind the shock wave is $[CF_3]_0$ The density ratio ρ_{21} is multiplied in Equation (8) to reference the event to laboratory time (t_ℓ). In calculating k_3 (expt'l) by means of Equation (8), γ was taken to be unity for the lower temperature data, and was assumed zero for the higher temperature data. Calculations (Figures 3 and 4) indicated that when analyzing the low temperature data after 50 percent decomposition, the above approximation was good to within 90 percent. Another feature brought out by the calculations was that after CF_3I and C_2F_6 chemical relaxation, the shock temperature profile was nearly constant, so that little temperature uncertainty was introduced in evaluating the rate constant for R3 during reaction. With the higher temperature data, k_3 (expt'l) was determined from the initial CF_2 absorption slope. As seen in Figure 5, the rather good agreement obtained within the scatter limits of k_3 (expt'l) in the CF_3I and C_2F_6 experiments tends to uphold the data reduction method. Examples of the CF_3I and C_2F_6 study are given in Table 2.

CF_4 Decomposition: In the temperature range 2200° to 3000° K, the CF_3 dissociation rate is three orders of magnitude faster than the rate of appearance of CF_2 in the oscillogram records of CF_4 decomposition. Hence these observations suggested that the rate determining step for CF_2 formation starting with CF_4 was R4. Calculations (Figure 6) showed that under the experimental conditions chosen the CF_3 concentration would be much less than that of CF_2 and CF_4 in the reaction mixture, allowing an apparent rate constant for R4 to be evaluated from the initial CF_2 slope measurements according to

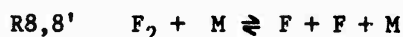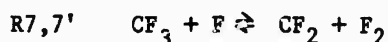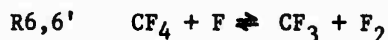$$\frac{d[CF_2]}{\rho_{21} \, dt_\ell} = k_4 \, (expt'l) \, \{[CF_4]_0 - [CF_2]\} \, [Ar]. \tag{9}$$

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Examples of the experiments are shown in Table 3. The temperature dependence of the apparent rate constants obtained from 1:100 and 2:100 CF_4-Argon gas mixtures is shown in Figure 7. The kinetic profile of CF_2 measured in a pure CF_4 run (Figure 8) is compared to that calculated from the nonequilibirum shocktube program using the rate constants in Table 1. The results indicate that the collision efficiencies of CF_4 and argon appear to be quite similar. Another aspect of the pure CF_4 experiment is that the intermediate CF_3 chemistry becomes important and serves as a check on its rate constants in the calculations. The rate constants for R5 and R5' were obtained in an earlier study of the thermal decomposition of the difluoromethylene radical[10].

Finally, for a number of shock conditions, measured and calculated kinetic profiles of CF_2 from decomposition of the three fluorocarbon molecules investigated are shown in Figure 9. It is seen that the rate constants given in Table 1 would appear to be adequate in describing the experimental data over the temperature range of the study.

DISCUSSION

The heat-of-reaction for R3 was obtained from JANAF thermochemical data and used to fit the experimental rate constants of the CF_3I and C_2F_6 data. The large temperature exponent ($T^{-9.04}$) determined appears to be inconsistent with the classical collision treatment for a polyatomic like CF_3. The maximum number of internal degrees of freedom not counting rotations which could contribute energy for reaction would be 6. Rotational and translational participation, if included, would increase the temperature exponent to only ($T^{-8.5}$). It was found that in calculating the CF_2 rate profiles, good agreement with the measurements could be obtained with the JANAF equilibrium constant multiplied by 16. With the equilibrium pre-exponential factor kept constant, a factor of 16 gives a heat-of-reaction of 81.2 kcal/mole at 2000° K (average temperature range of data). By refitting the rate constants of R3 with the revised heat-of-reaction, a temperature exponent of ($T^{-6.21}$) is obtained, which is more in accord with theory.

Besides the reactions shown in Table 1, the rate data were also analyzed by adding the reactions

$$R6,6' \qquad CF_4 + F \rightleftharpoons CF_3 + F_2$$

$$R7,7' \qquad CF_3 + F \rightleftharpoons CF_2 + F_2$$

$$R8,8' \qquad F_2 + M \rightleftharpoons F + F + M$$

Calculations based on rate constants from classical collision theory and JANAF equilibrium constants showed that R6,6' and R7,7' were about three orders of magnitude slower than the decomposition reactions and had negligible effect on the measured CF_2 kinetic profiles.

ACKNOWLEDGEMENTS

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APPENDIX A

Formulation of the Nonequilibrium Shock-Tube Program

The nonequilibrium shock tube program solves simultaneously the Rankine-Hugoniot conservation relations and the chemical rate equations expressing variation in species concentration. The program is organized to integrate the rate equations stepwise, an iteration scheme to satisfy the conservation relations being repeated at each step. It differs from the average ordinary differential equation program chiefly in that the equations themselves are not fixed. Instead, only rules for generating the equations are fixed.

The input quantities include the shock velocity; the temperature, pressure, and species mole fractions ahead of the shock; the chemical reactions to be considered; the preexponential factor, temperature exponent, and activation energy of the rate constant for each reaction; and coefficients of the enthalpy curve fits. A library tape of species data (molecular weights and enthalpy fit coefficients) may be searched for quantities omitted from the regular program input. The chemical reactions are entered directly in equation form, a maximum of four species allowed on each side of an equation, with each species allotted a maximum of eight alpha-numeric characters. For example, consider the simple system

$$C2F4 + M = CF2 + CF2 + M$$

$$CF2 + CF2 + M = C2F4 + M$$

$$CF2 + M = CF + F + M$$

$$CF + F + M = CF2 + M$$
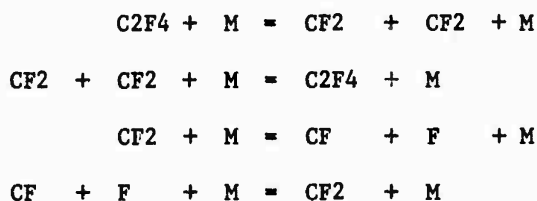
where M will be taken by convention to refer to the sum of all species concentrations.

The set of equations is analyzed by the program, the species in each equation matched against an input list of all species occurring in the problem, and a matrix M of indices set up to represent the original equations. If, in the example above, the species are arbitrarily ordered,

C2F4   CF2   CF   F

1   2   3   4

and M is assigned the index 5, the 4x8 matrix generated by the program is

$$M = \begin{bmatrix} 1 & 5 & 0 & 0 & 2 & 2 & 5 & 0 \\ 2 & 2 & 5 & 0 & 1 & 5 & 0 & 0 \\ 2 & 5 & 0 & 0 & 3 & 4 & 5 & 0 \\ 3 & 4 & 5 & 0 & 2 & 5 & 0 & 0 \end{bmatrix}$$

The rules for generating the set of differential equations are then as follows:

For the ith species the change in the concentration $C_i(t)$ as a function of time is defined as

$$\frac{d}{dt} C_i(t) = \sum_{j=1}^{N_R} R_j (\delta_{l_j} + \delta_{r_j}) \prod_{K=1}^{4} C_{M_{j,K}} \qquad i = 1, \ldots, N_S$$

where

N_S is the number of species

N_R is the number of reactions

R_j is the rate constant corresponding to the jth equation

$$\delta_{l_j} = \begin{cases} -n & \text{if the } i^{th} \text{ species occurs } n \text{ times on the left side of equation } j \\ \\ o & \text{if the } i^{th} \text{ species does not occur on the left side of equation } j \end{cases}$$

$$\delta_{r_j} = \begin{cases} +n & \text{if the } i^{th} \text{ species occurs } n \text{ times on the right side of equation } j \\ \\ o & \text{if the } i^{th} \text{ species does not occur on the right side of equation } j \end{cases}$$

and by definition

$$C_o = 1$$

$$C_{N_S + 1} = \sum_{i=1}^{N_S} C_i$$

Again, for the example, the equations are

$$\frac{d}{dt} C_1 = (-R_1 C_1 + R_2 C_2^2) \sum_{i=1}^{4} C_i$$

$$\frac{d}{dt}\ C_2\ =\ (\ 2\ R_1\ C_1\ -\ 2\ R_2\ C_2{}^2\ -\ R_3\ C_2\ +\ R_4\ C_3\ C_4\,)\ \sum_{i=1}^{4}\ C_i$$

$$\frac{d}{dt}\ C_3\ =\ (\ R_3\ C_2\ -\ R_4\ C_3\ C_4\,)\ \sum_{i=1}^{4}\ C_i$$

$$\frac{d}{dt}\ C_4\ =\ (\ R_3\ C_2\ -\ R_4\ C_3\ C_4\,)\ \sum_{i=1}^{4}\ C_i$$

To find initial conditions for the system of differential equations, the con-
servation relations are first solved for values of the temperature $T_2(0)$ and
density $\rho_2(0)$. A false position iteration for temperature is used in the solution.
Then, since the mole fractions $X_i(t)$ are known (input) quantities at time 0,
the concentrations may be found from the relation

$$C_i(t)\ =\ \frac{X_i(t)\ \rho_2(t)}{\displaystyle\sum_{i=1}^{N_S}\ X_i(t)\ M_i}\qquad\qquad i=1,\ldots,N_S$$

where M_i is the molecular weight of the ith species.

To solve the differential equations a fourth order predictor-corrector method,
sometimes called the Modified Adams-Bashforth Method, is used. This method is
generally available for computer use in an Avco library subroutine which was
partially reprogrammed for purposes of the problem. The technique is particu-
larly attractive because of its computational efficiency and the relative ease
it affords in maintaining accuracy requirements. The one major disadvantage is
that it is not self-starting.

Before the predictor-corrector algorithm can even be applied, values of all the
concentrations $C_i(t)$, $i=1,\ldots,N_S$ and of their first derivatives $\frac{d}{dt}\ C_i(t)$, $i=1,\cdots,N_S$

must be known at each of four points in time. Information at the first point
$t_o=0$ can be obtained directly from the initial conditions. Values at three
additional equally-spaced points t_1, t_2, and t_3 are obtained by a fourth order
Runge-Kutta integration process, the interval Δt between the points being con-
trolled by program input. Runge-Kutta is particularly appropriate as a starting
method since results at each step depend only on conditions at the last previous
step. In addition, a high degree of accuracy can be established with a suffi-
ciently small interval. (However, Runge-Kutta would present serious disadvantages
if used over the entire time period. A relatively large number of derivative

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calculations are required, and no immediate estimate of the truncation error is available.) In the fourth order Runge-Kutta method the derivatives are evaluated at four points in the interval and weighted to give agreement with a Taylor Series expansion through the fourth order term. For a comprehensive discussion of Runge-Kutta integration see chapter 9 in __Mathematical Methods for Digital Computers__, edited by Ralston and 'ilf[6].

Given the starting values obtained from Runge-Kutta, the predictor-corrector algorithm operates as follows. For each concentration C_i, $i = 1, \ldots, N_s$, a third degree polynomial $\widetilde{P}_i(t)$ approximating $d/dt\, C_i$ is fitted through the four available derivative values. This polynomial is then integrated to give an exprapolated or predicted concentration

$$\widetilde{C}_i(t_4) = C_i(t_3) + \int_{t_3}^{t_4} \widetilde{P}_i(t)\, dt \qquad i = 1, \ldots, N_s$$

at $t_4 = t_3 + \Delta t$ From the set $\widetilde{C}_i(t_4)$, $i = 1, \ldots, N_s$ approximate derivatives $d/dt\, \widetilde{C}_i(t_4)$ are calculated directly. Then a new polynomial $\overline{P}_i(t)$ is fitted through $d/dt\, C_i(t_1)$, $d/dt\, C_i(t_2)$, and $d/dt\, C_i(t_3)$, and $d/dt\, \widetilde{C}_i(t_4)$, and interpolated or corrected concentrations

$$\overline{C}_i(t_4) = C_i(t_3) + \int_{t_3}^{t_4} \overline{P}_i(t)\, dt \qquad i = 1, \ldots, N_s$$

are computed.

Since the truncation errors for the extrapolation and interpolation formulas are of the same order, the difference $\overline{C}_i(t_4) - \widetilde{C}_i(t_4)$ provides an estimate of the actual truncation error incurred by the integration scheme in the interval from t_3 to t_4. In fact, it can be shown that, neglecting higher order terms, the true value $C_i(t_4)$ lies between $\overline{C}_i(t_4)$ and $\widetilde{C}_i(t_4)$. Again, see reference (6), chapter 8 for a general discussion of predictor-corrector techniques.

In the algorithm the quantity $|\overline{C}_i(t_4) - \widetilde{C}_i(t_4)|$ is tested to ensure that the integration is sufficiently accurate. A relative tolerance specified through program input, multiplied by $\sum_{i=1}^{N_s} C_i(0)$, is taken as an absolute upper limit for $|\overline{C}_i(t_4) - \widetilde{C}_i(t_4)|$. If for any i this limit is exceeded, the time interval Δt is halved and the integration retried. The process of testing, cutting the interval, and reapplying the predictor-corrector step is repeated until $|\overline{C}_i(t_4) - \widetilde{C}_i(t_4)|$ is sufficiently small. Then the predicted values $\widetilde{C}_i(t_4)$, $i = 1, \ldots, N_s$ are taken as the result of integration, and $d/dt\, \widetilde{C}_i(t_4)$, $i = 1, \ldots, N_s$ as the set of corresponding derivatives. (The predicted rather than the corrected results are accepted to avoid computing the additional set of derivatives.) If, for each i, $|\overline{C}_i(t_4) - \widetilde{C}_i(t_4)|$ is at least one hundred times smaller than the limiting criterion, the

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interval Δt will be doubled before the next integration step is begun. The whole process is then repeated over successive intervals, at each step the latest Δt and conditions at the last four points entering the computation, until the end of the time period is reached.

The program was coded in FORTRAN IV for use on the IBM 360 series of computers. Execution times for typical problems on the 360 model 75 computer range between one and two minutes.

TABLE I

FLUOROCARBON REACTIONS AND RATE CONSTANTS[a]

R1 $CF_3I + M \rightarrow CF_3 + I + M$	$k_1 = 2.27 \times 10^{30} \, T^{-4.0} \exp(-57385/RT)$
R2 $C_2F_6 + M \rightarrow CF_3 + CF_3 + M$	$k_2 = 8.40 \times 10^{20} \, T^{0.5} \exp(-76500/RT)$
R2' $CF_3 + CF_3 + M \rightarrow C_2F_6 + M$	$k_2' = 7.14 \times 10^{17} \, T^{0.5}$
R3 $CF_3 + M \rightarrow CF_2 + F + M$	$k_3 = 1.57 \times 10^{49} \, T^{-9.04} \exp(-92254/RT)$
R3' $CF_2 + F + M \rightarrow CF_3 + M$	$k_3' = 1.49 \times 10^{46} \, T^{-9.04} \exp(-2287/RT)$
R4 $CF_4 + M \rightarrow CF_3 + F + M$	$k_4 = 6.15 \times 10^{34} \, T^{-4.64} \exp(-122421/RT)$
R4' $CF_3 + F + M \rightarrow CF_4 + M$	$k_4' = 9.79 \times 10^{31} \, T^{-4.64} \exp(-2849/RT)$
R5 $CF_2 + M \rightarrow CF + F + M$	$k_5 = 4.20 \times 10^{26} \, T^{-2.85} \exp(-106000/RT)$
R5' $CF + F + M \rightarrow CF_2 + M$	$k_5' = 6.57 \times 10^{26} \, T^{-2.85}$
M = collision partner (Argon)	

[a]units in calories, cubic centimeter, degree Kelvin, mole, second.

TABLE 2

EXAMPLES OF CF_3I AND C_2F_6 SHOCK TUBE EXPERIMENTS

Experiment No.	Shock Velocity (mm/μ sec)	[a]Shock Temp. (°K)	$P21$	Total Gas Conc'n (mole/cm^3) 10^6	Apparent Rate Constant (k_3, cm^3/mole sec)
		1:100 CF_3I – Argon Data			
1	1.322	1804	3.66	7.94	2.28×10^8
2	1.382	1928	3.75	8.16	9.08×10^8
3	1.441	2060	3.82	8.33	4.95×10^9
4	1.478	2143	3.87	8.45	5.08×10^9
5	1.510	2214	3.92	8.56	7.73×10^9
		1:100 C_2F_6 – Argon Data			
6	1.347	1735	4.00	10.8	9.09×10^7
7	1.395	1850	4.02	8.72	5.69×10^8
8	1.440	1960	4.03	8.76	1.20×10^9
9	1.456	2000	4.04	8.76	1.38×10^9
10	1.533	2205	4.06	8.82	4.88×10^9

[a]conditions for complete dissociation of CF_3I and C_2F_6 at shock front.

TABLE 3

EXAMPLES OF CF$_4$ SHOCK TUBE EXPERIMENTS

Experiment No.	Shock Velocity (mm/μsec)	[a]Shock Temp. ($^\circ$K)	ρ_{21}	Gas Conc'n (mole/cm^3)10^5	Apparent Rate Constant (k$_4$,cm^3/mole sec)
		1:100 CF$_4$ – Argon Data			
11	1.559	2410	3.75	1.82	7.96 x 10^7
12	1.623	2590	3.78	1.63	3.32 x 10^8
13	1.643	2640	3.795	1.42	5.61 x 10^8
14	1.670	2720	3.808	0.518	1.04 x 10^9
15	1.715	2850	3.83	0.422	1.89 x 10^9
[a]16	1.795	2970	4.05	1.09	4.70 x 10^9
		2:100 CF$_4$ – Argon Data			
17	1.507	2260	3.81	1.84	2.91 x 10^7
18	1.544	2350	3.845	1.76	6.12 x 10^7
19	1.591	2460	3.87	1.67	1.34 x 10^8
20	1.623	2550	3.89	1.57	3.63 x 10^8
21	1.66	2650	3.91	1.39	8.20 x 10^8
		CF$_4$ Data			
22	2.015	2145	19.1	0.515	5.10 x 10^6
23	2.075	2248	19.4	0.521	2.42 x 10^7

[a]Rate constant evaluated at 40 percent decomposition.
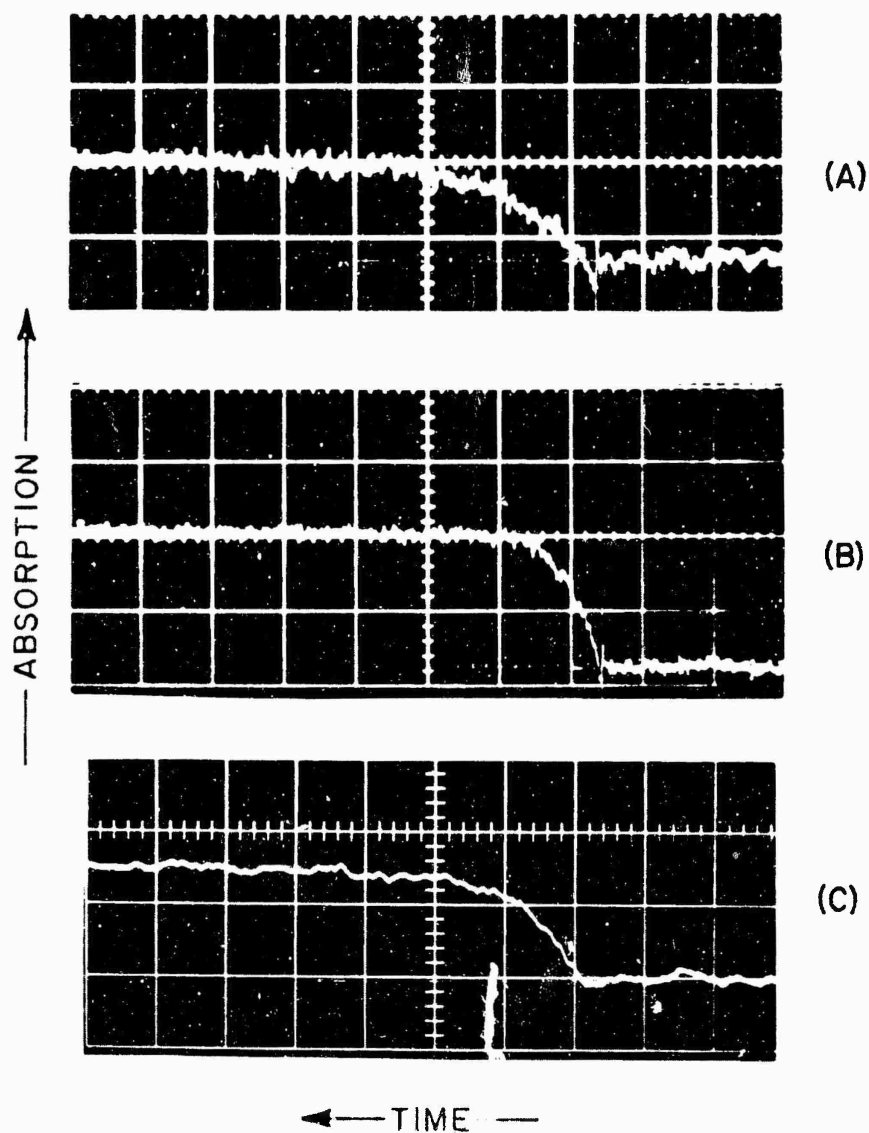
27-3651

Figure 1 Difluoromethylene ultraviolet light absorption
behind shock waves into

(a) 1:100 CF$_3$I-Ar, shock veloc. = 1.377 mm/μsec, Temp = 1984° K

(b) 1:100 C$_2$F$_6$-Ar, shock veloc. = 1.456 mm/μsec, Temp = 2107° K

(c) 1:100 CF$_4$-Ar, shock veloc. = 1.782 mm/μsec, Temp = 3050° K

at 4 cm Hg initial pressure. Oscillogram writing = 20 μsec/cm

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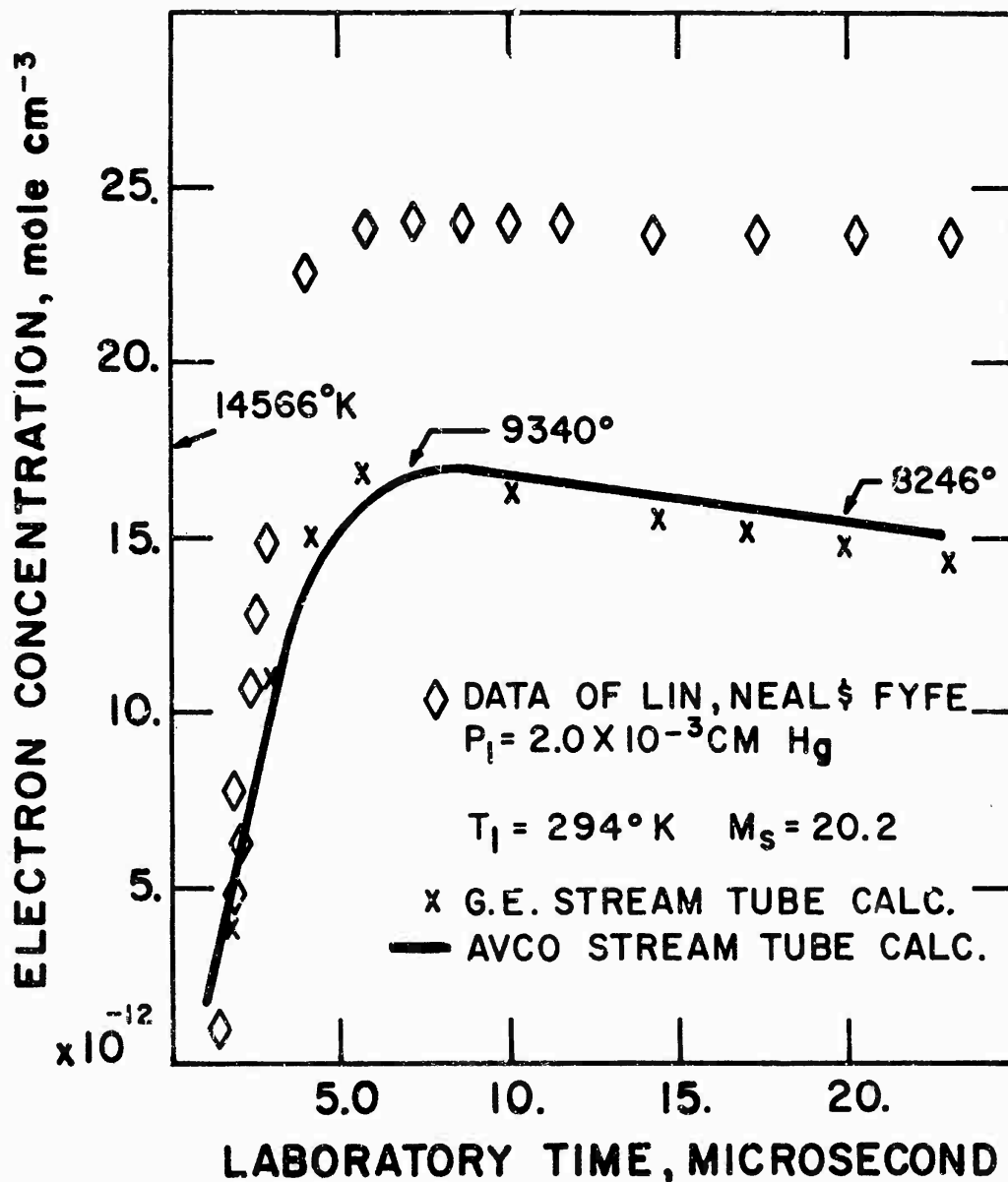
Figure 2 Numerical Check of Nonequilibrium Shock-Tube
Program with Airchemistry Stream-Tube Calculation.
◊, ["Rate of Ionization Behind Shock Waves in Air.
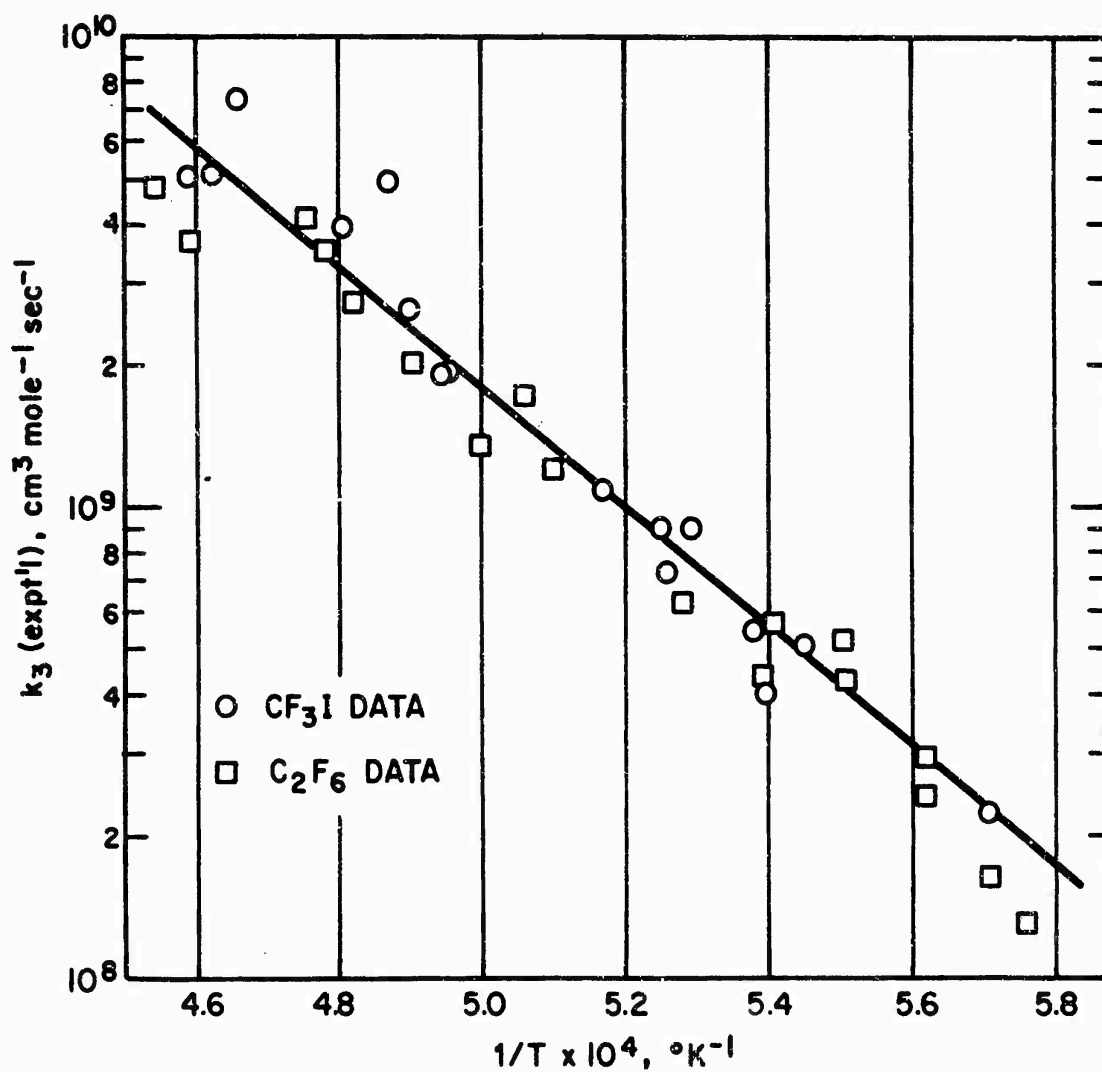I. Experimental Results," Avco/Everett Research
Rept. 105, (September, 1960)] .
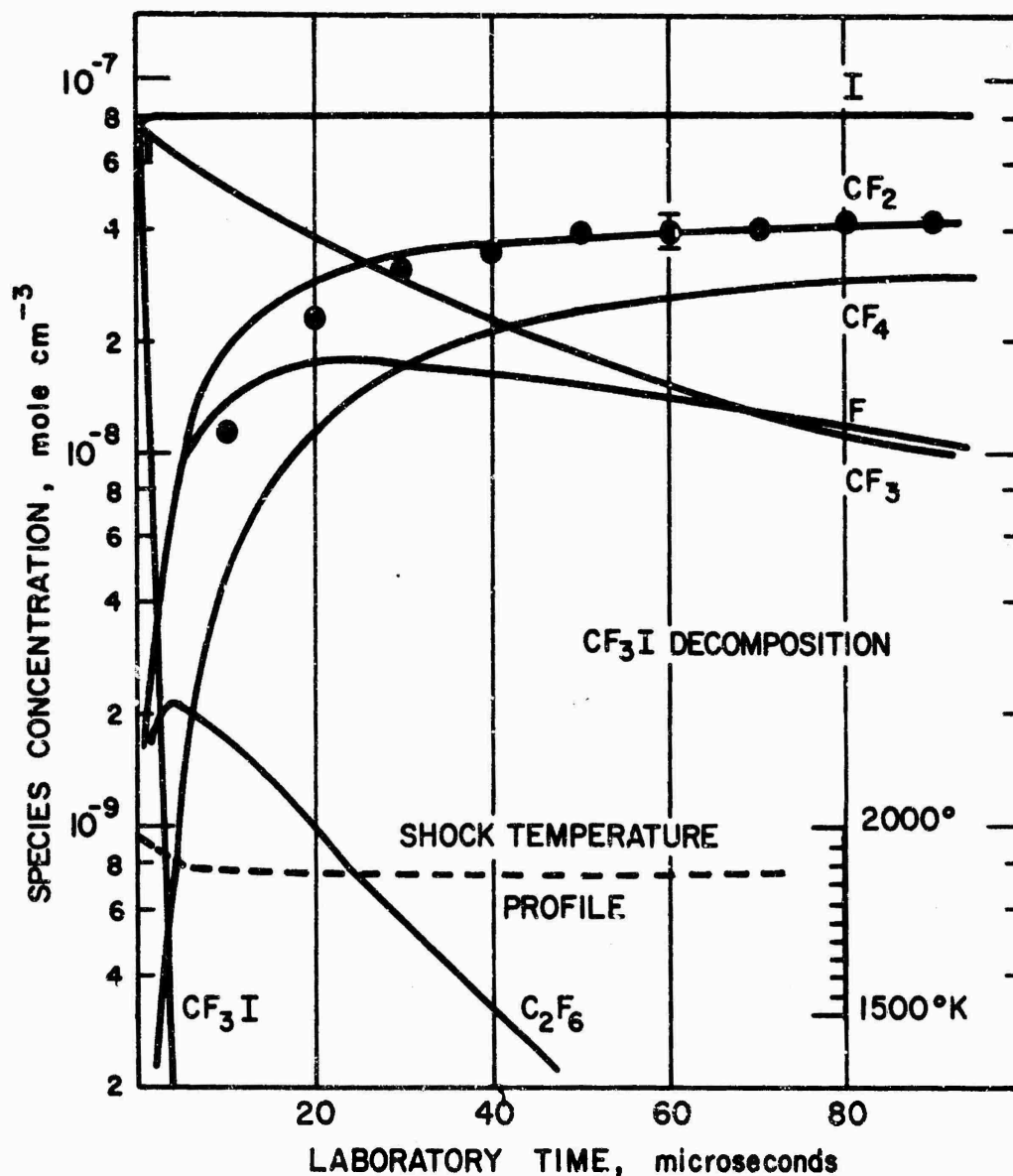
Figure 3 Chemical kinetics shock-tube calculation for
decomposition of 1:100 CF_3I-Argon gas mixture
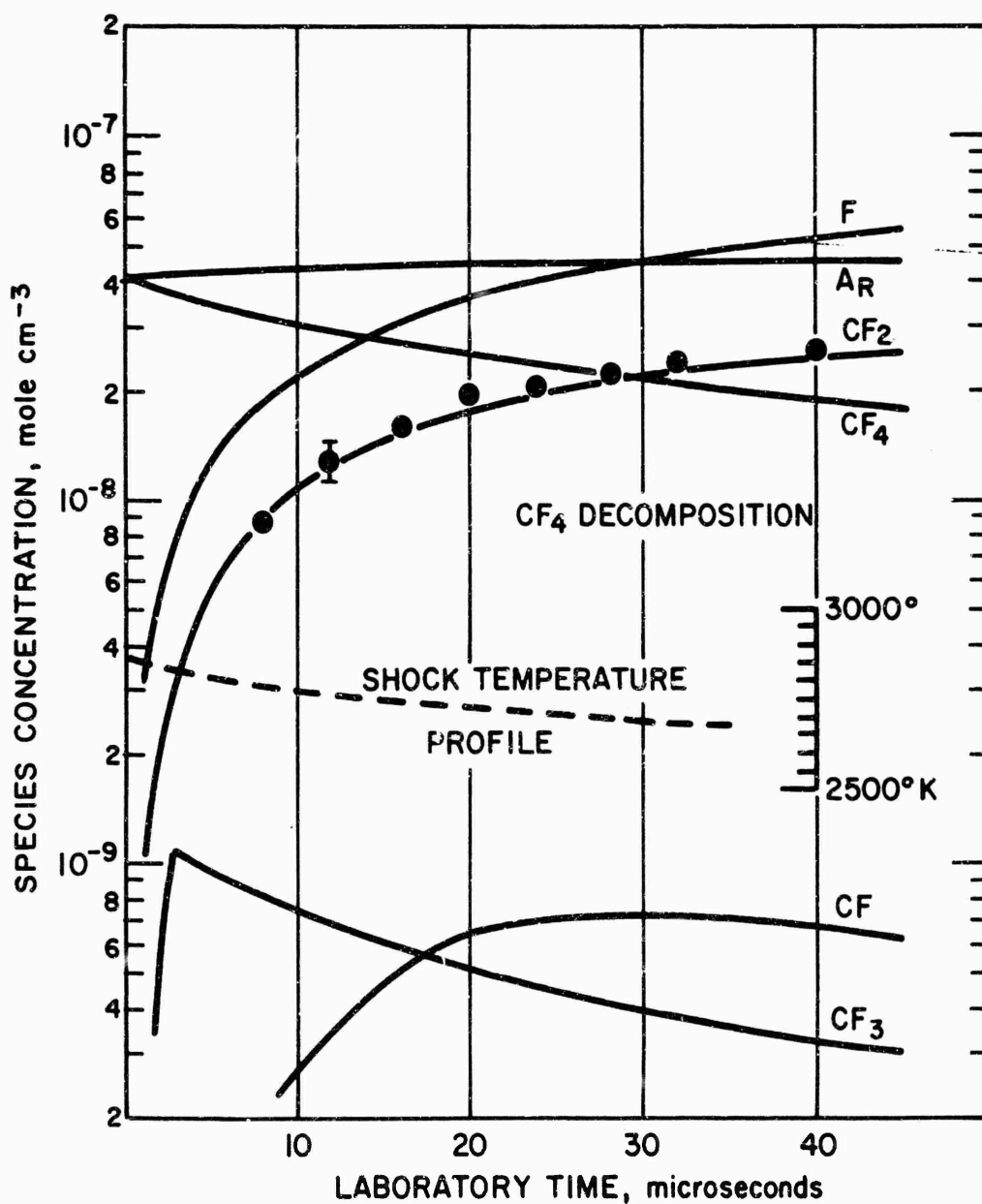(Experiment No. 2). ⊙, spectroscopic
measurements of CF_2 concentration. Error flag
reflects uncertainty in absorption coefficient used in
data reduction. Argon curve is (100) I.
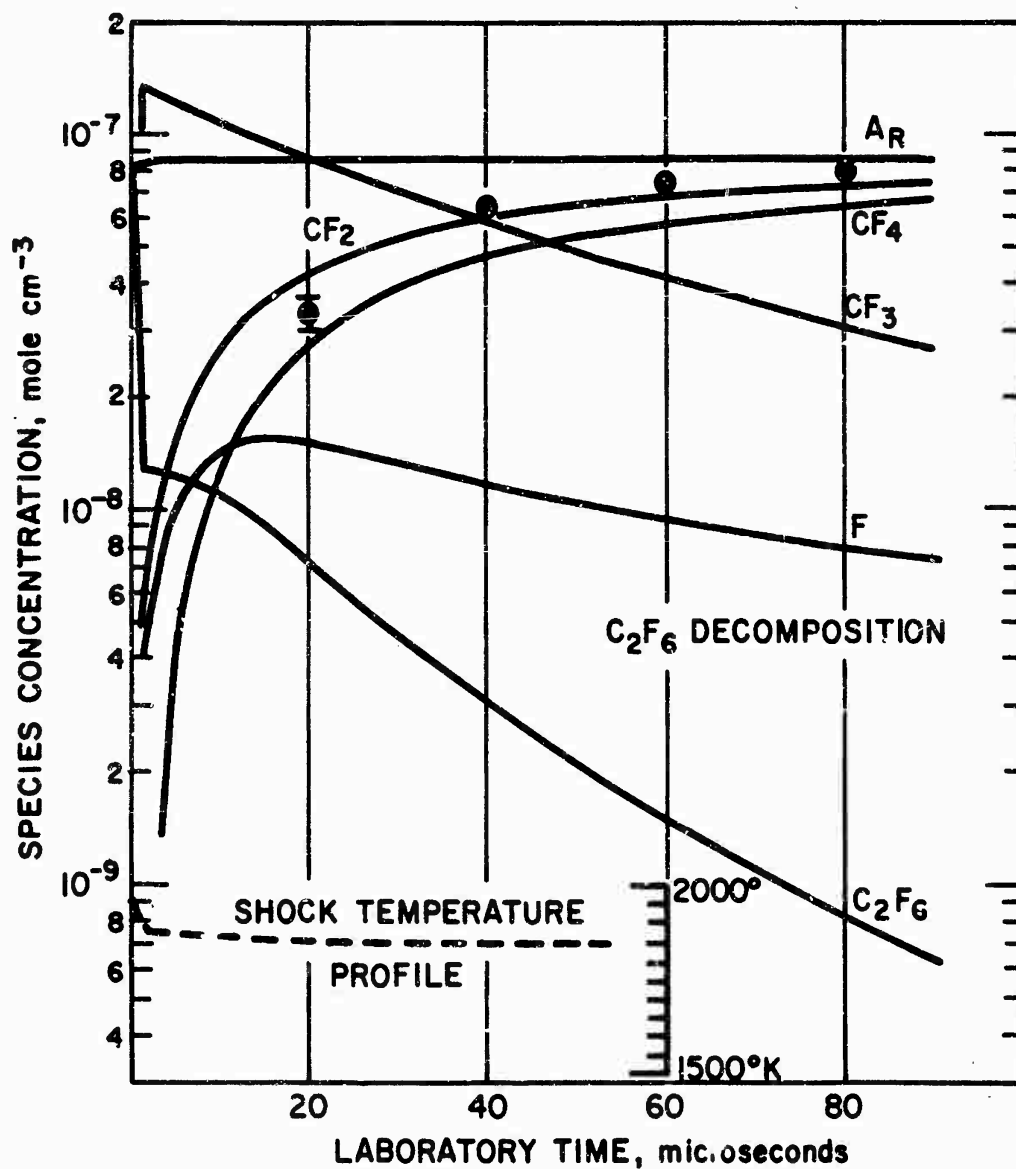
27-3644

27-3645

Figure 4 Chemical kinetics shock-tube calculation for
decomposition of 1:100 C_2F_6 - Argon gas mixture
(Experiment No. 7). ⊙, spectroscopic measure-
ments of CF_2 concentration.

27-3647

Figure 5   Experimental rate constant for CF_3 dissociation.
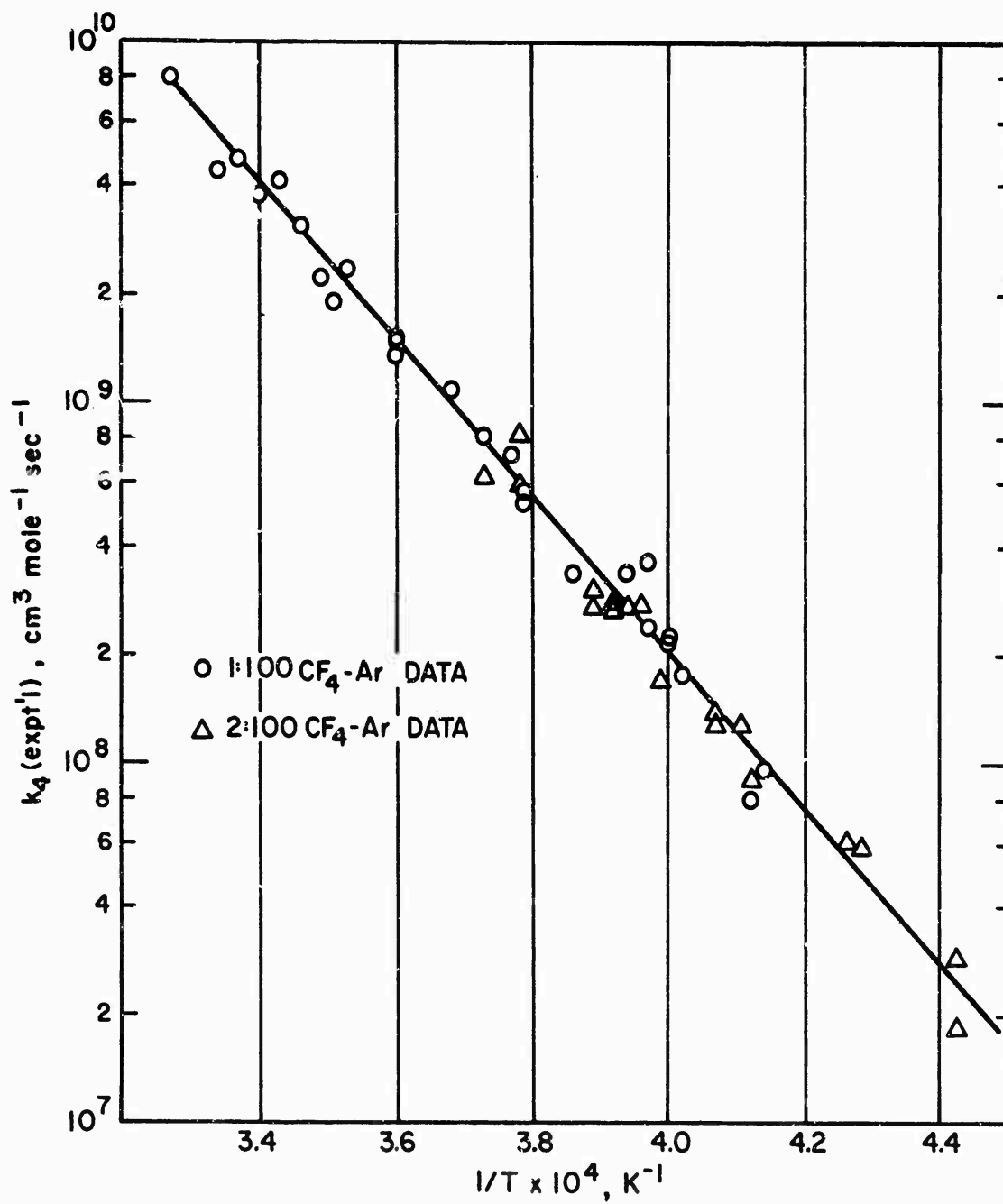Solid line is the function

$$1.57 \times 10^{49} \, T^{-9.04} \, \exp(-92254/RT)$$

$cm^3 \, mole^{-1} \, sec^{-1}$ from least squares fit of data.

Figure 6 Chemical kinetics shock-tube calculation for
decomposition of 1:100 CF_4 - Argon gas mixture
(Experiment No. 15). ⊙, spectroscopic measure-
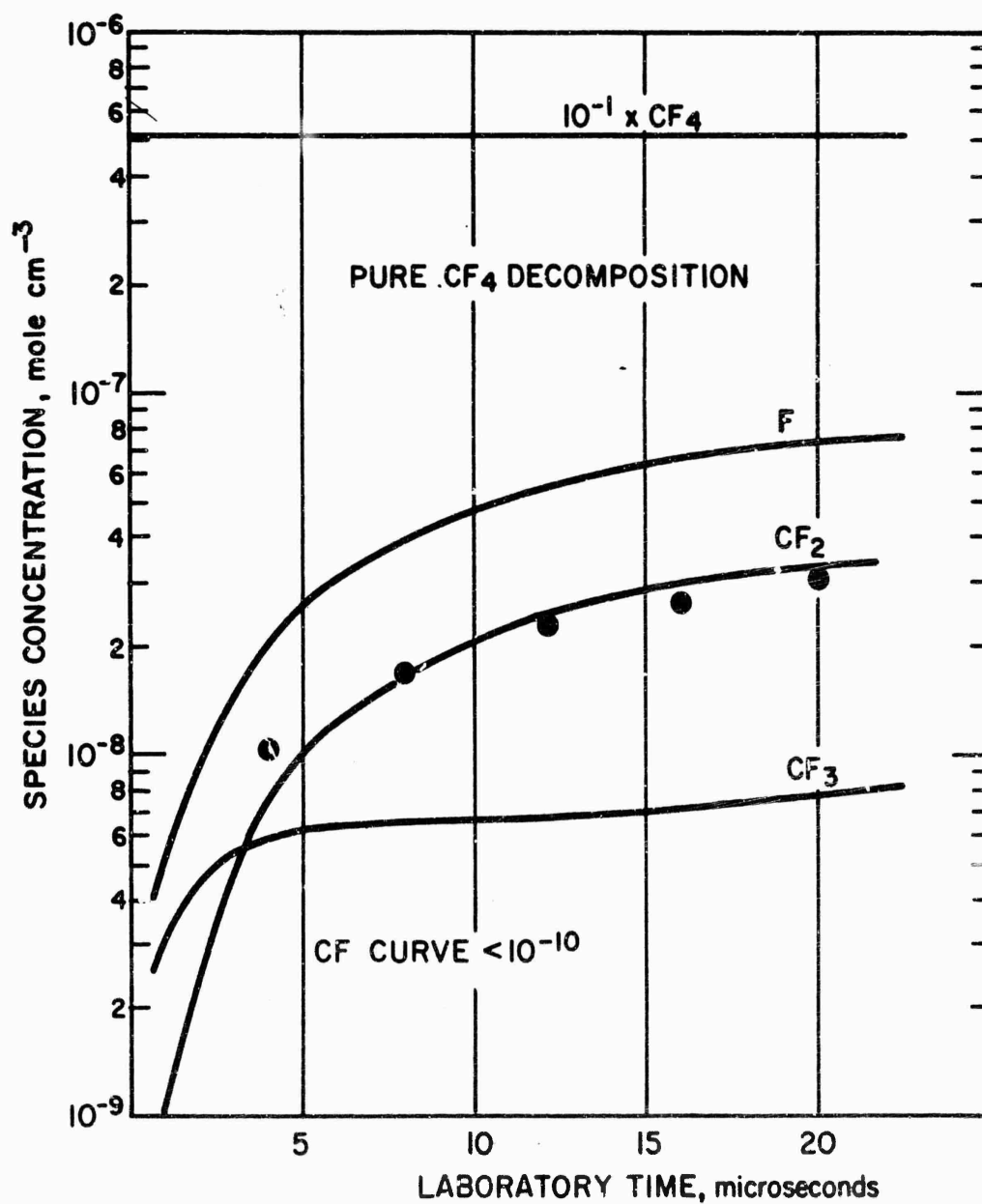ments of CF_2 concentration.

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Figure 7 Experimental rate constant for CF_4 dissociation.
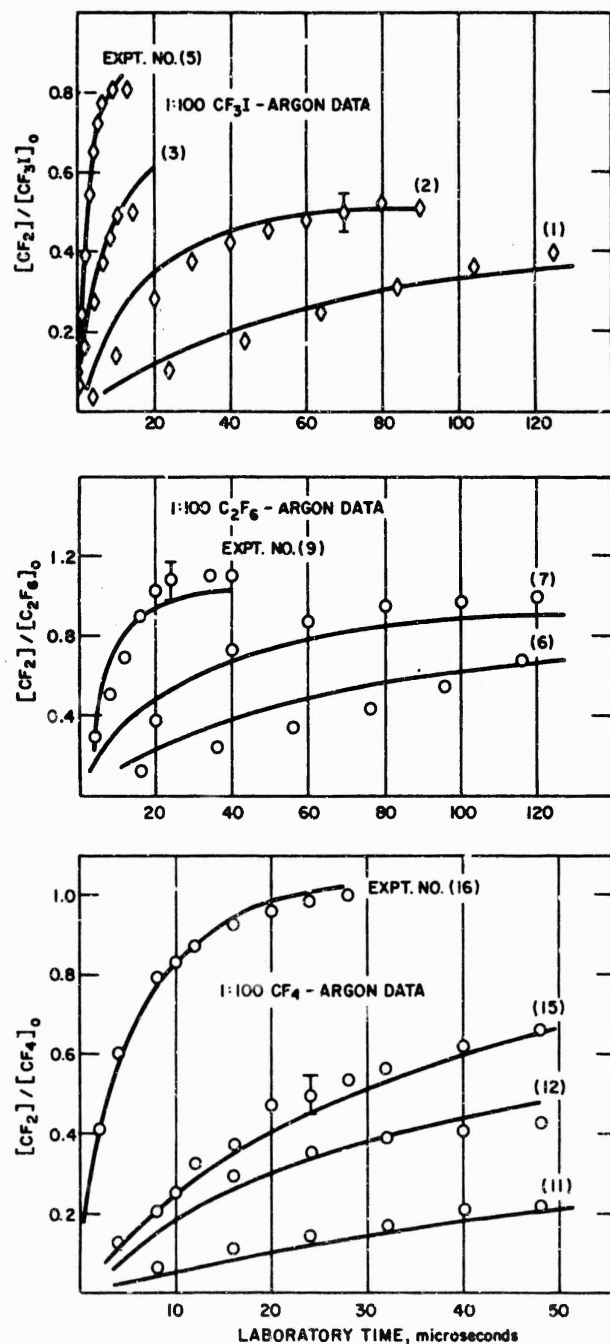Solid line is the function

$$6.15 \times 10^{34} \, T^{-4.64} \, \exp(-122421/RT)$$

$cm^3 \, mole^{-1} \, sec^{-1}$ from least squares fit of data.

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Figure 8 Chemical kinetics shock-tube calculation
for decomposition of pure CF_4
(Experiment No. 22). $\odot$, spectroscopic
measurements of CF_2 concentration in
reaction mixture.

27-3646

Figure 9 Kinetic profiles of CF_2 in shock heated fluorocarbon-argon gas mixtures. Curves are calculated by the nonequilibrium shock-tube program. Symbols are spectroscopic measurements. Subscript 0 denotes reactant concentration initially behind shock wave.